



# **Changing the Radio Station**

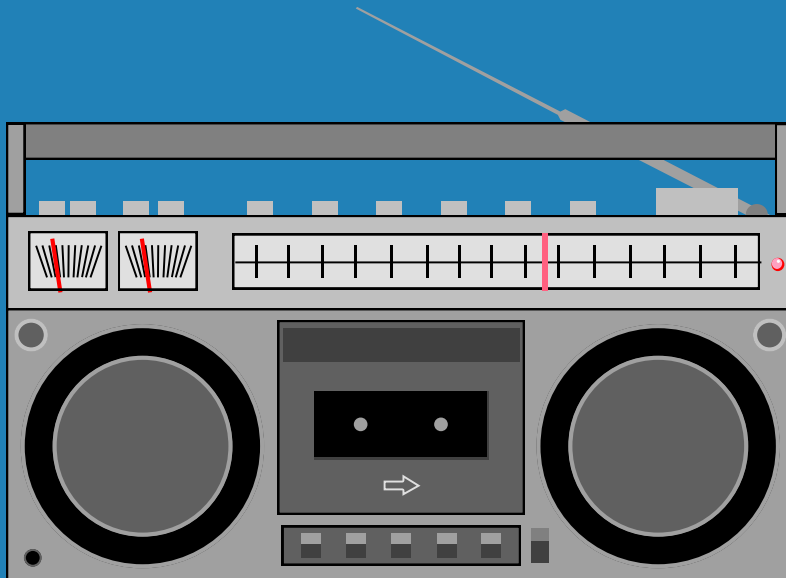
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**Lori Davis**

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# Radio Signals



Radio Signals

Stations:  $S_1, S_2, \dots, S_x$

$f_1(t) + f_2(t) + \dots + f_x(t)$

# Station Signals

∩  $h(t) * \sin(nt)$

∩ **AM signal =  $h(t)$**

∩ **carrier signal =  $\sin(nt)$**

# Types of Signals

## ∩ AM Signals

∩  $S_1 = 3\sin(nt) - 2\sin(2t)$

∩  $S_2 = 5\sin(nt) - 6\sin(2t)$

∩  $S_3 = 4\sin(nt) - 7\sin(2t)$

## ∩ Carrier Signals

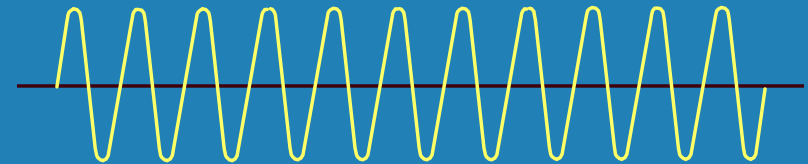
∩  $S_1 = \sin(8t)$

∩  $S_2 = \sin(16t)$

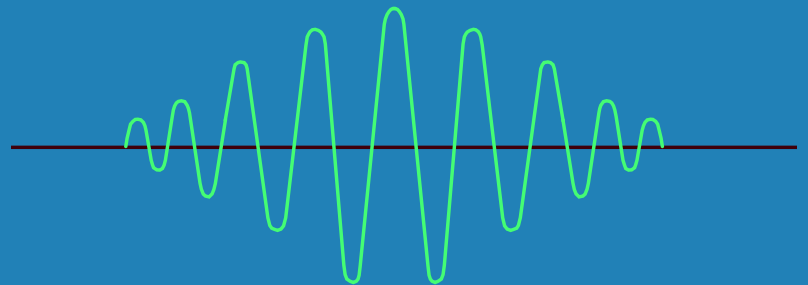
∩  $S_3 = \sin(24t)$

# Complete Signals

⌚  $S_1 = (3\sin t - 2\sin(2t)) * [\sin(8t)]$



⌚  $S_2 = (5\sin t - 6\sin(2t)) * [\sin(16t)]$



⌚  $S_3 = (4\sin t - 7\sin(2t)) * [\sin(24t)]$

# Computation

$$\mathcal{Q} \mathbf{f}(t) = \mathbf{S}_1 + \mathbf{S}_2 + \mathbf{S}_3$$

$$\int_0^{\Pi} f(t) * \cos(17t) dt$$

$$\int_0^{\Pi} f(t) * \cos(18t) dt$$

# Generalized Solution

$$\int_0^{\Pi} f(t) * \cos(n + p) \, dt$$

# Jean Baptiste Joseph Fourier



∞ Heat Flow

∞ Spatial Rate



# Spatial Rate of Change

- ∂ Heat conductivity of the object
- ∂ Initial temperature distribution on the object's boundary
- ∂ Object's geometric shape

# Fourier Series

∴  $h(t) =$   
 $a_1 \sin(t) + a_2 \sin(2t)$   
 $+ a_3 \sin(3t) + \dots$

∴ **Fourier Sine Series**

∴ **Fourier Cosine Series**

∴ **Complete Fourier Series**



# Computation

$$\int_0^{\Pi} h(t) * \sin(nt) dt$$

$$= a_n * \int_0^{\Pi} \sin^2(nt) dt$$

$$= a_n * \frac{\Pi}{2}$$

$$A_n = \frac{2}{\Pi} \int_0^{\Pi} h(t) * \sin(nt) dt$$



# Summary

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- ∩ **Terms in a Fourier Series**
- ∩ **Trigonometric Functions with Calculus**
- ∩ **Applications in other fields**